

B.Tech Degree IV Semester Examination, April 2010

**ME 403 ADVANCED MECHANICS OF SOLIDS
(2006 Scheme)**

Time: 3 Hours

Maximum Marks: 100

**PART - A
(Answer ALL questions)**

(8 x 5 = 40)

- I. (a) Explain Saint Venant's principle.
- (b) Explain the concept of principal stresses. Mention its significance in practical problems.
- (c) Obtain the stress distribution of the solid disk in rotation with uniform thickness.
- (d) Draw the stress diagrams in composite tubes.
- (e) Explain Lamé's stress ellipsoid.
- (f) Explain Castigliano's first theorem.
- (g) Explain concept of shear center.
- (h) Explain membrane analogy.

311

297

37

160

112

262

PART - B

(4 x 15 = 60)

- II. (a) Derive equations of equilibrium in 3-D in most general form.
- (b) Draw the Mohr's circle for the following stresses and graphically find out principal stresses and maximum shear stress.

(8)

$$\tau_{xx} = 4000 \text{ KPa} \quad \tau_{yy} = 1000 \text{ KPa} \quad \tau_{xy} = -500 \text{ KPa}$$

(7)

OR

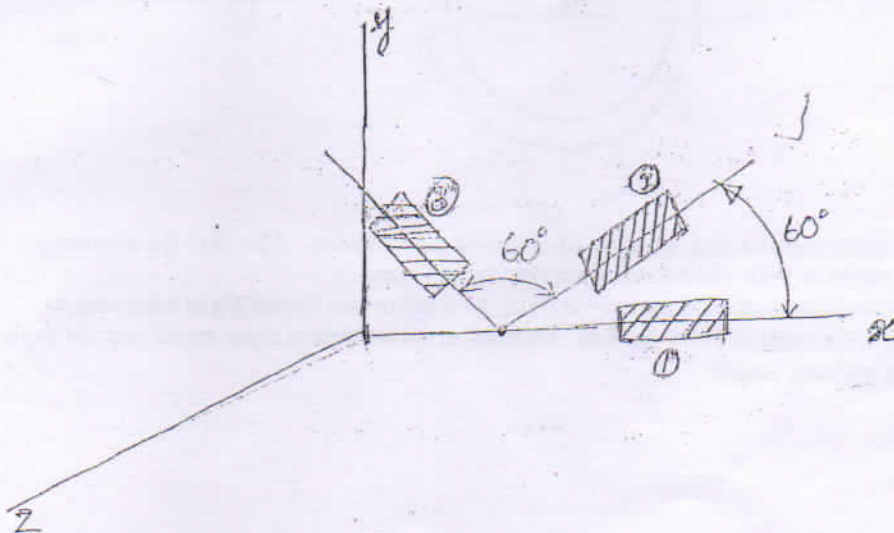
- III. (a) Explain compatibility conditions. From this concept obtain compatibility equations in strain terms.
- (b) Using a 60° strain rosette the following strains have been determined at a point on the surface of a steel of a machine base.

(8)

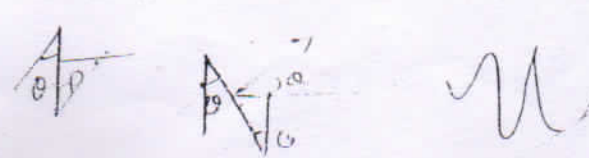
$$E_1 = 40 \mu \quad E_2 = 980 \mu \quad E_3 = 330 \mu$$

Determine strain components in 3 rectangular co-ordinates and principal strains and maximum shearing strain.

(7)



(Turn Over)



- IV. Derive an equation for the contact pressure for a shrink fitted composite tubes in terms of shrink fit allowance. (15)

OR

- V. *m* A steel turbine rotor of 750mm outer diameter, 150mm inner diameter and 50mm thickness has 100 blades 150mm long each weighing 4N. It is shrink fitted on a rigid shaft. Calculate the initial shrinkage allowance on the inner diameter of the rotor so that it just loosens on the shaft at 3000 revolutions per minute. Assume $E=200$ GPa and Poisson's ratio 0.3. The density of the shaft and rotor is 7500 kg/m^3 . (15)

- VI. (a) Derive displacement equations of equilibrium. (7)
 (b) The following is the stress matrix at a point P. Determine the principal stresses and their associated directions.

$$[\tau_{ij}] = \begin{bmatrix} 1 & 2 & 1 \\ 2 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix} \quad (8)$$

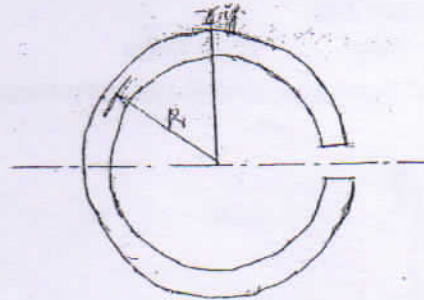
OR

- VII. (a) Derive the relation for the strain energy due to shear and bending. $\rightarrow (162)$ (9)
 (b) Determine the deflection at end A of cantilever beam shown in figure. (6)



(165)

- VIII. Determine the shear stress distribution for a circular open section under bending caused by a shear force. Also locate the shear center. (15)



(219)

OR

- IX. (a) Obtain the stresses acting on a bar of elliptical cross section. Also find the maximum stress, angle of twist and torsional rigidity for the same. (10)
 (b) An elliptical shaft of semi axes $a = 0.05\text{m}$, $b = 0.025\text{m}$ and $G = 80\text{GPa}$ is subjected to a twisting moment of $1200 \pi \text{ N.m}$. Determine the maximum shear stress and the angle of twist per unit length. (5)
